



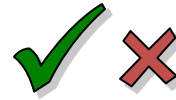
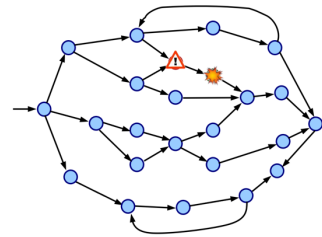
PRISM

ETAPS Test-of-Time Tool Award 2024

Marta Kwiatkowska, Gethin Norman, [Dave Parker](#)

What is PRISM?

- PRISM: Probabilistic (symbolic) model checker

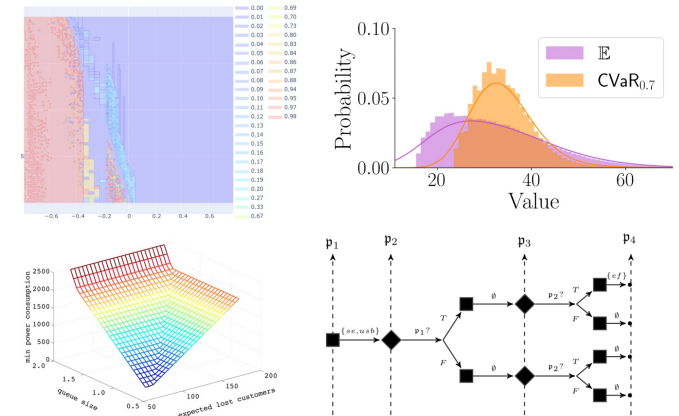


$$P_{>p} [\square (\triangle \rightarrow \diamond \leq k \star)]$$

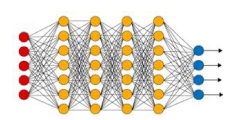
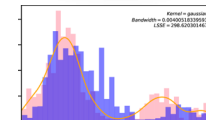
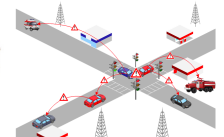
- PRISM today

- 12 types of probabilistic models, many probabilistic temporal logics
- uses: logic, automata, Markov models, optimisation, SMT, simulation, game theory, artificial intelligence, learning...
- >400 case studies across a broad range of application domains

- PRISM development: driven by challenges, applications, users

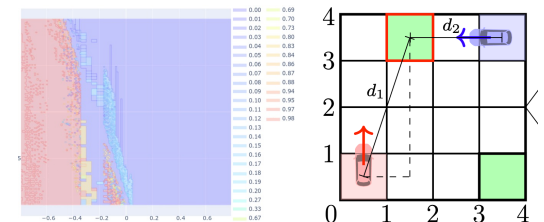
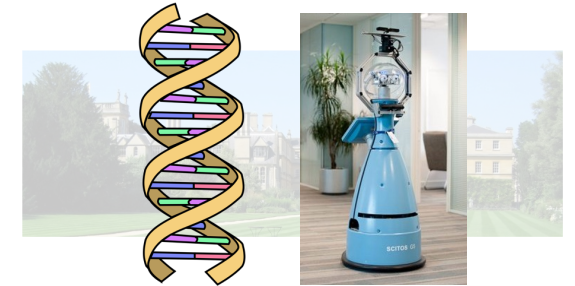


CTMC, CSG,
DTMC, LTS, MDP,
POMDP, POPTA,
PTA, STPG, SMG,
TPTG, IDTMC,
IMDP



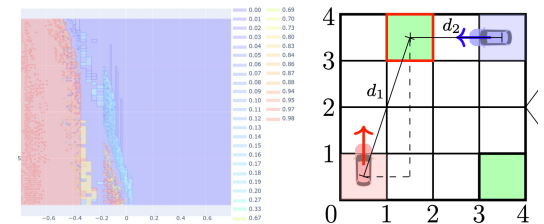
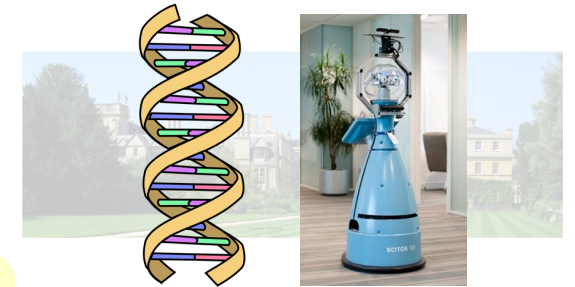
PRISM: A brief history

- 1998: tool development begins (Birmingham)
 - symbolic probabilistic model checking
- 2001: first official public release of PRISM
- 2004 & 2006: PRISM 2.0 & 3.0
 - new GUI, logics, cost/reward models, simulator engines
- 2011: PRISM 4.0
 - probabilistic real-time systems, PRISM benchmark suite
 - multi-objective model checking & assume-guarantee
- 2013: first release of PRISM-games
- 2016 & 2020: PRISM-games 2.0 & 3.0
 - multi-objective, concurrent stochastic games, equilibria
- 2020-2024: policy/strategy synthesis, POMDPs, uncertain MDPs, ...



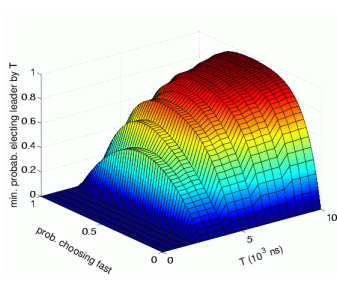
PRISM: A brief history

- 1998: tool development begins (Birmingham)
 - symbolic probabilistic model checking [TACAS'00,'02]
- 2001: first official public release of PRISM
- 2004 & 2006: PRISM 2.0 & 3.0 [TACAS'06]
 - new GUI, logics, cost/reward models, simulator engines [TACAS'04]
- 2011: PRISM 4.0
 - probabilistic real-time systems, PRISM benchmark suite
 - multi-objective model checking & assume-guarantee [TACAS'07,'10,'11]
- 2013: first release of PRISM-games [TACAS'12,'13]
- 2016 & 2020: PRISM-games 2.0 & 3.0
 - multi-objective, concurrent stochastic games, equilibria [TACAS'15,'16,'22]
- 2020-2024: policy/strategy synthesis, POMDPs, uncertain MDPs, ...

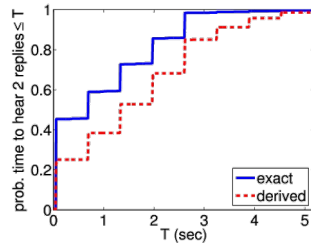


Early applications of PRISM

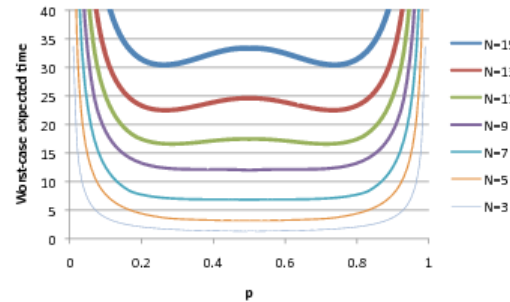
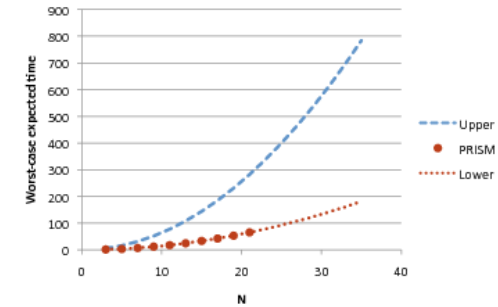
- Randomised distributed algorithms/protocols
 - modelled as MDPs/probabilistic automata
 - key motivating example for probabilistic verification



FireWire protocol

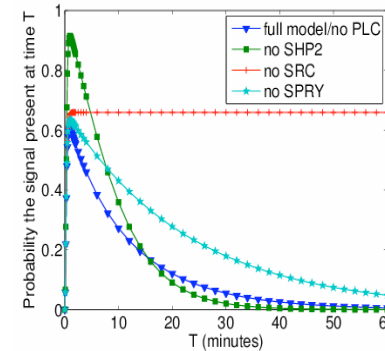


Bluetooth device discovery

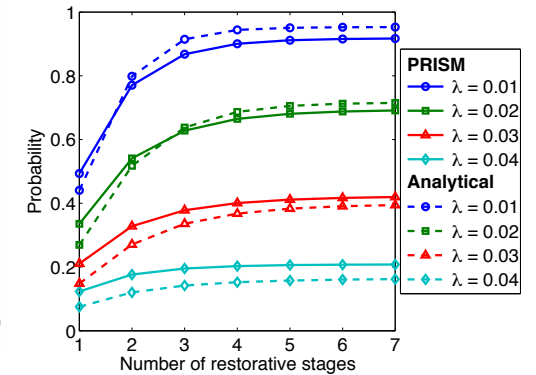


Herman's self-stabilisation

- Performance modelling & biochemical reactions
 - modelled as Markov chains



FGF cell signalling pathway experiments



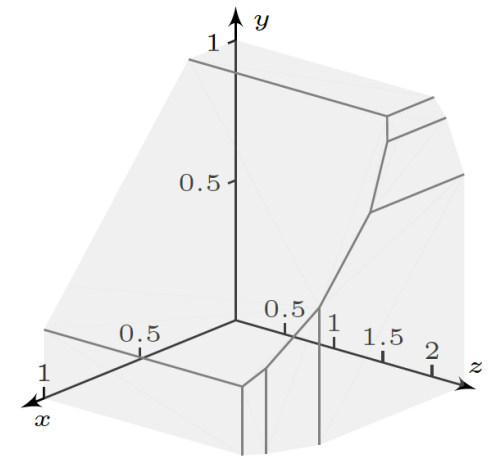
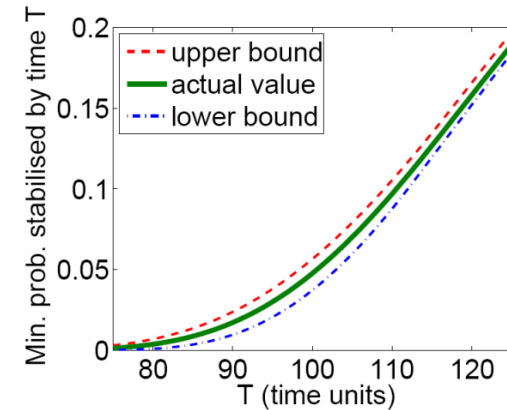
Reliable multiplexing in nanotechnology

Multiple flaws, bugs, anomalies found...

Enabling technologies

- Challenge-driven tool development

- Symbolic model checking
 - [TACAS'00] [TACAS'02] [STTT'04] [CAV'06] ...
 - Real-time probabilistic verification
 - [TCS'02] [FMSD'06] [Info&Comp'07] [FORMATS'09] ...
 - Game-based abstraction refinement
 - [QEST'06] [VMCAI'09] [FMSD'10] [QEST'11] ...
 - Multi-objective & compositional verification
 - [TACAS'10] [QEST'10] [FASE'11] [Info&Comp'13] ...
 - Multi-agent model checking (stochastic games)
 - [TACAS'12] [Inf-&Comp'17] [FMSD'21] [TACAS'22] ...



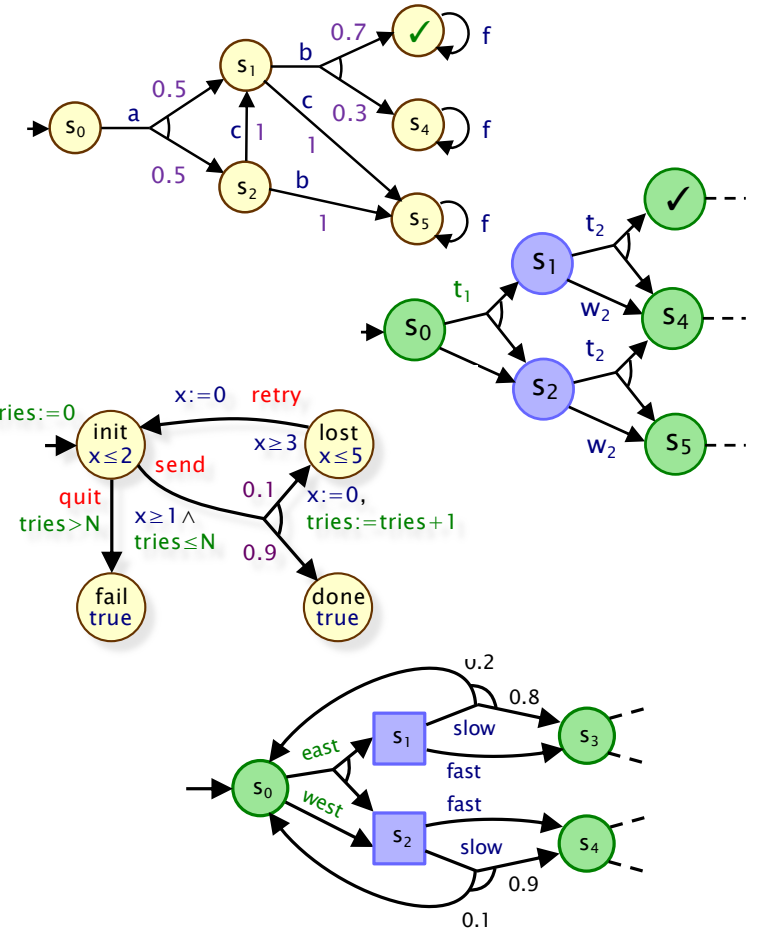
$$\begin{array}{c}
 M_1 \models \langle A \rangle_{\geq q} \\
 \langle A \rangle_{\geq q} M_2 \langle G \rangle_{\geq p} \\
 \hline
 M_1 \parallel M_2 \models \langle G \rangle_{\geq p}
 \end{array}$$

PRISM models

- Increasing variety (and complexity) of **probabilistic models** supported

- discrete-time Markov chains
- probabilistic automata
- continuous-time Markov chains
- Markov decision processes (MDPs)
- probabilistic timed automata
- partially observable MDPs
- stochastic multi-player games
- concurrent stochastic games
- interval Markov chains & MDPs

- + concurrency
- + exponential delays
- + policies / control
- + real-time clocks
- + observability
- + multi-agent & strategies
- + concurrency & equilibria
- + epistemic uncertainty



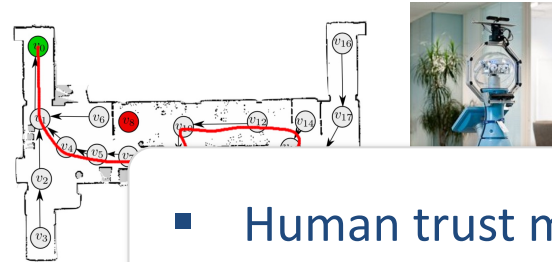
PRISM applications

- Increasing variety (and complexity) of **applications** tackled

From verification
to control problems

- discrete-time Markov chains
- probabilistic automata
- continuous-time Markov chains
- Markov decision processes
- probabilistic timed automata
- partially observable MDPs
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- interval Markov chains & MDPs

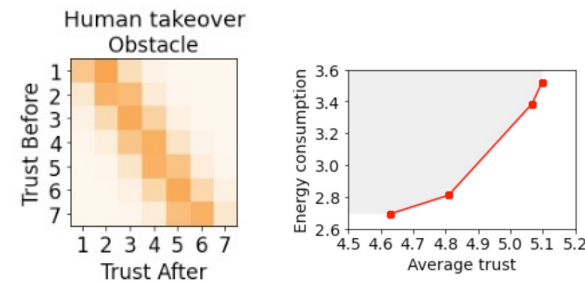
- Long-running autonomous mobile robots [IJRR'19]
 - via multi-objective MDPs



- Real-time task scheduling with faulty processors [FMSD'13]
 - probabilistic timed automata

time	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
task5																				
task6																				
task4																				
task																				
task																				
task																				
task4																				
task5																				
task-d																				

- Human trust models for automated driving [TCPS'22]
 - via multi-objective POMDPs



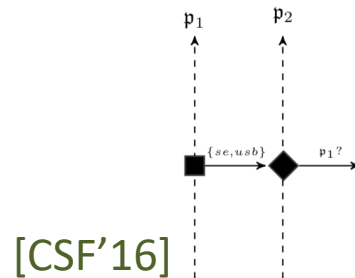
PRISM applications

- Increasing variety (and complexity) of applications tackled

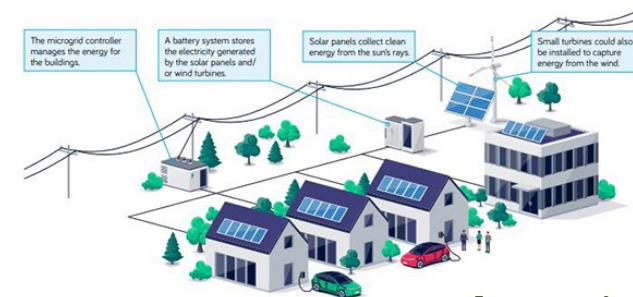
Verification
+ game theory

- discrete-time Markov chains
- probabilistic automata
- continuous-time Markov chains
- Markov decision processes
- probabilistic timed automata
- partially observable MDPs
- stochastic multi-player games
- concurrent stochastic games
- interval Markov chains & MDPs

- Computer security attack-defence scenarios
 - stochastic games strategies



- Distributed energy protocols
 - flaws fixed via incentives



[FMSSD'13]

PRISM applications

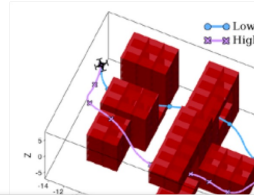
- Increasing variety (and complexity) of **applications** tackled

Verification & epistemic uncertainty

- discrete-time Markov chains
- probabilistic automata
- continuous-time Markov chains
- Markov decision processes
- probabilistic timed automata
- partially observable MDPs
- stochastic multi-player games
- concurrent stochastic games
- interval Markov chains & MDPs

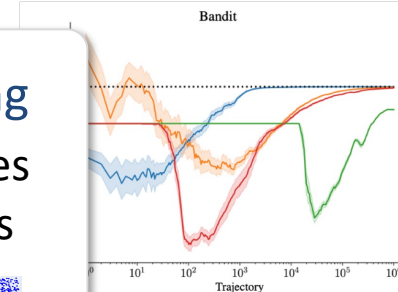
- Robust AUV control [JAIR'23]

- continuous-space + unknown noise \rightarrow IMDP



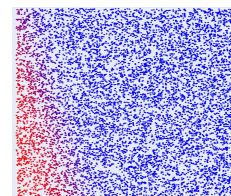
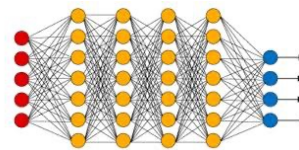
- Robust anytime learning [NeurIPS'22]

- MDP policies learnt from samples
- IMDPs used for robust guarantees




- Deep reinforcement learning

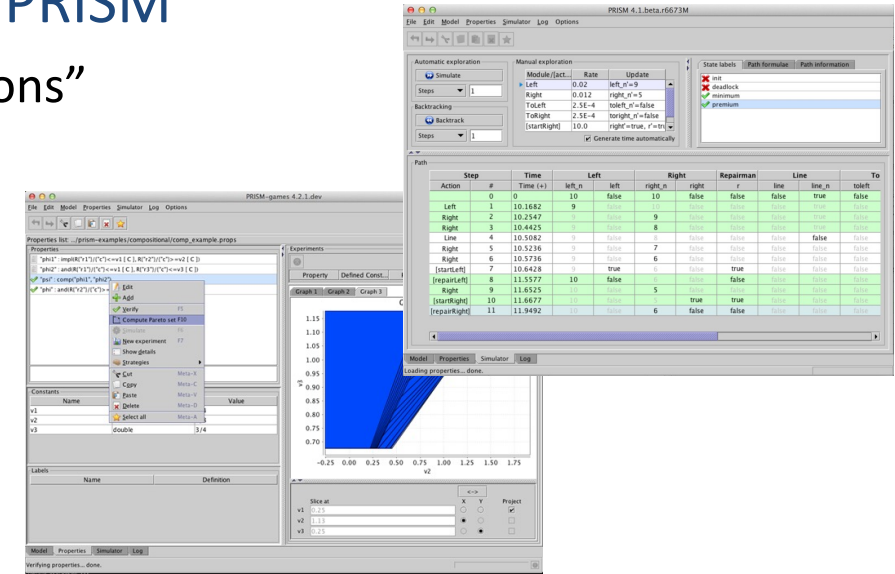
- verified probabilistic policies from neural nets, via IMDPs



[FORMATS'22]

Who uses PRISM? (and how/why)

- PRISM bibliography¹ lists >850 papers relating to PRISM
 - 375 “case studies”, >100 “extensions”, >250 “connections”
- PRISM applications & users
 - very wide (often non-expert) user base
 - broad applicability of PMC techniques/models
 - easy, self-contained install 
 - user interface: model editor, simulator, debugger, graph plotting, ...
 - documentation, tutorials, examples
- General aims
 - stable, usable, flexible, coherent framework



• PRISM for teaching

- common basis for the practical component of taught courses on (non-)probabilistic model checking


¹ <https://prismmodelchecker.org/bib.php>

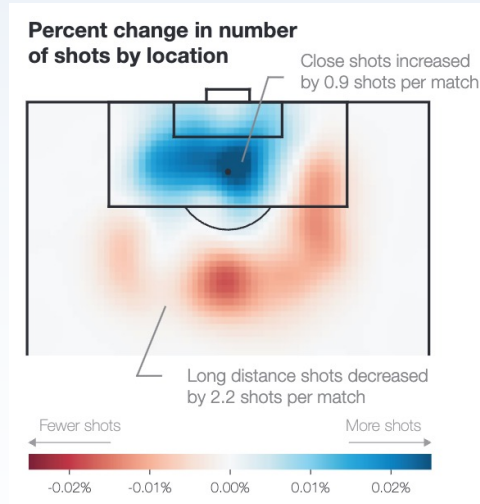
Diverse applications of PRISM

- Cloud computing
 - live migration of VMs
 - plan optimisation for performance guarantees



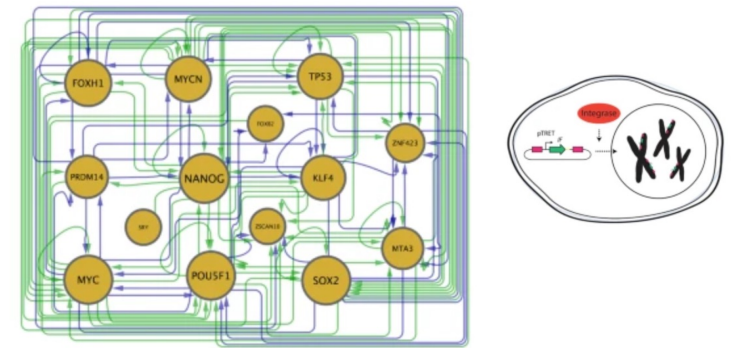
[Kikuchi/Matsumoto
(Fujitsu), CLOUD'11]
(Best paper)

- Football tactics 
 - team strategies learnt from data
 - tactical efficiency analysed via probabilistic model checking



[Van Roy et al.,
JAIR'23, MIT-SSAC'24]



- Human-cell conversion
 - for disease models, gene therapies
 - design tool for optimisation and prediction, based on model checking

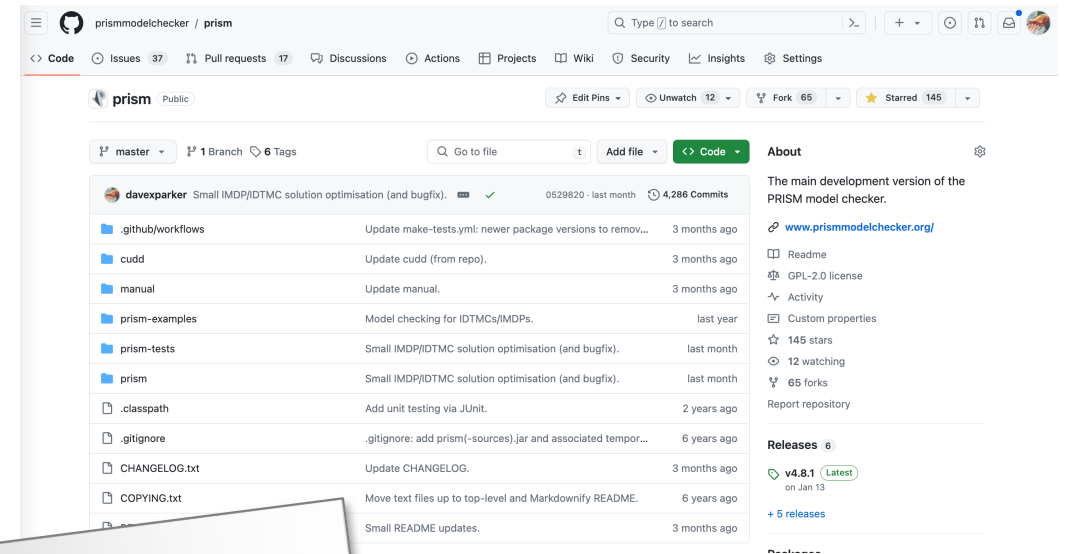


[Jung et al., Nature
Communications'21]

Building on PRISM

- Extending PRISM

- open-source codebase (GPL) 
- primarily implemented in Java 
 - (some C code and various native libraries)
- accessibility for student/external contributors
 - “explicit” engine is an easy entry point



- Connections & tool chains

- via PRISM modelling language
 - e.g. PEPA, bigraphs, RoboChart, SBML
- via explicit (textual) model files
- programmatically via API
 - Java, Python, model generators



The PRISM language

- PRISM modelling language
 - simple textual language based on guarded commands
 - inspired by: SMV language, Reactive modules
 - de-facto standard for probabilistic verification
- Key ingredients
 - the basics: modules (variables + guarded commands), parallel composition, costs/rewards, parameters (constants)
 - also: clocks, observations, players, epistemic uncertainty, ...
- Some design decisions
 - consistent modelling language for many model types
 - (deliberately) simple/low-level, general-purpose language

```
csq
player p1 user1 endplayer
player p2 user2 endplayer
// Users (senders)
module user1
  s1 : [0..1] init 0; // has player 1 sent?
  e1 : [0..emax] init emax; // energy level of player 1
  [w1] true -> (s1'=0); // wait
  [t1] e1>0 -> (s1'=c' ? 0 : 1) & (e1'=e1-1); // transmit
endmodule
module user2 = user1 [ s1=s2, e1=e2, w1=w2, t1=t2 ] endmodule
// Channel: used to compute joint probability distribution for transmission failure
module channel
  c : bool init false; // is there a collision?
  [t1,w2] true -> q1 : (c'=false) + (1-q1) : (c'=true); // only user 1 transmits
  [w1,t2] true -> q1 : (c'=false) + (1-q1) : (c'=true); // only user 2 transmits
  [t1,t2] true -> q2 : (c'=false) + (1-q2) : (c'=true); // both users transmit
endmodule
```

CTMC, CSG,
DTMC, LTS, MDP,
POMDP, POPTA,
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The PRISM language

- PRISM modelling language

- simple textual language based on guarded commands
- inspired by: SMV language
- de-facto standard

- Key ingredients

- the basics: module
parallel composition
- also: clocks, observations

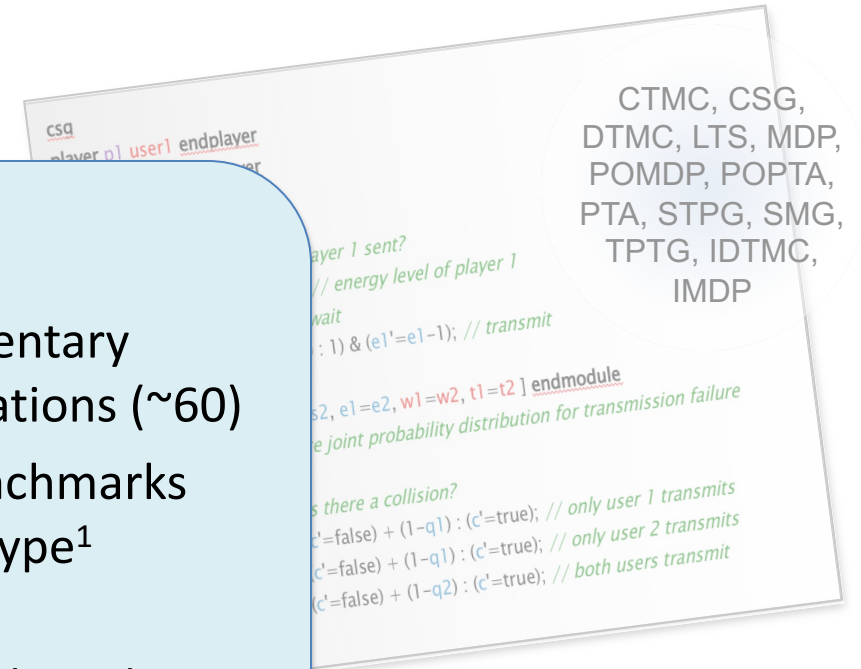
- PRISM models as benchmarks

- open data: >15 years of supplementary materials pages on PRISM publications (~60)
- benchmark suite: 36 scalable benchmarks & property queries classified by type¹

¹ See also: Quantitative Verification Benchmark Set

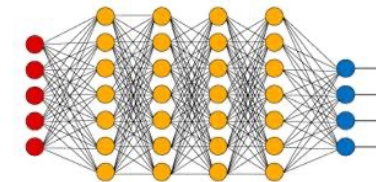
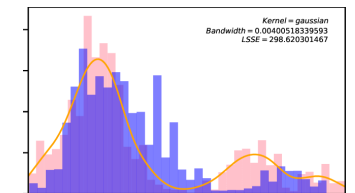
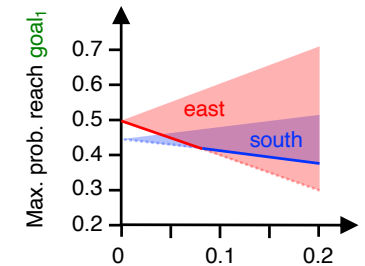
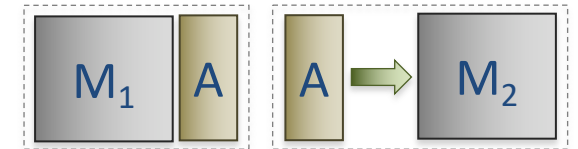
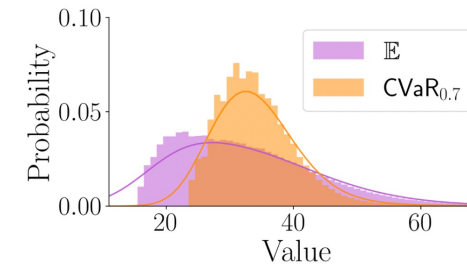
- Some design decisions

- consistent modelling language for many model types
- (deliberately) simple/low-level, general-purpose language



PRISM: Where next?

- Coming soon (ish) to PRISM
 - modelling/property language extensions
 - more flexible compositional model specifications
 - improved API access (Java, Python, ...)
 - better tool interoperability
- Research advances in model checking functionality
 - epistemic uncertainty (e.g., intervals)
 - learning models/parameters from data,
 - neuro-symbolic models
 - stochastic games & equilibria



Summary

- PRISM (& PRISM-games)
 - approx. 25 years of continuous development
 - challenge-, application- and user-driven tool evolution
 - stable, usable, coherent framework for wide user base
 - many enhancements to come and challenges to tackle

PRISM contributors:

Aistis Simaitis, Alberto Puggelli, Alistair John Strachan, Alessandro Bruni, Andrew Hinton, Carlos Bederian, Charles Harley, Chris Novakovic, Christian von Essen, Christoph Weinhuber, Clemens Wiltsche, Dave Parker, Edoardo Bacci, Ernst Moritz Hahn, Frits Dannenberg, Gabriel Santos, Gethin Norman, Hongyang Qu, Ingy Elsayed-Aly, Joachim Klein, Joachim Meyer-Kayser, Kenneth Chan, Ludwig Pauly, Mark Kattenbelt, Marta Kwiatkowska, Mateusz Ujma, Max Kurze, Mike Arthur, Nishan Kamaleson, Paolo Ballarini, Rashid Mehmood, Sebastian Vermehren, Steffen Märcker, Stephen Gilmore, Vincent Nimal, Vojtech Forejt, Xueyi Zou, Zak Cohen

(and many more contributors to underlying theory and techniques)



prismmodelchecker.org

PRISM supporters:

